

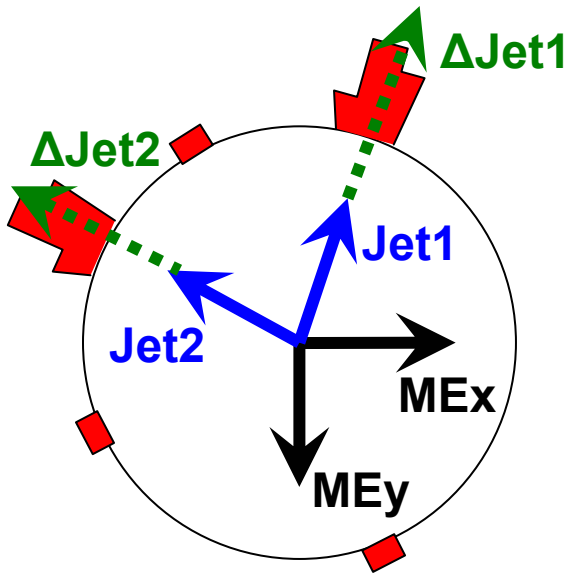
Missing Energy and New Physics

Amit Lath

Rutgers, the State University of NJ

What is MET?

$$\begin{aligned}\mathbf{E}_T^{\text{miss}} &= -\sum (E_n \sin \theta_n \cos \phi_n \hat{\mathbf{i}} + E_n \sin \theta_n \sin \phi_n \hat{\mathbf{j}}) \\ &= E_x^{\text{miss}} \hat{\mathbf{i}} + E_y^{\text{miss}} \hat{\mathbf{j}}\end{aligned}$$

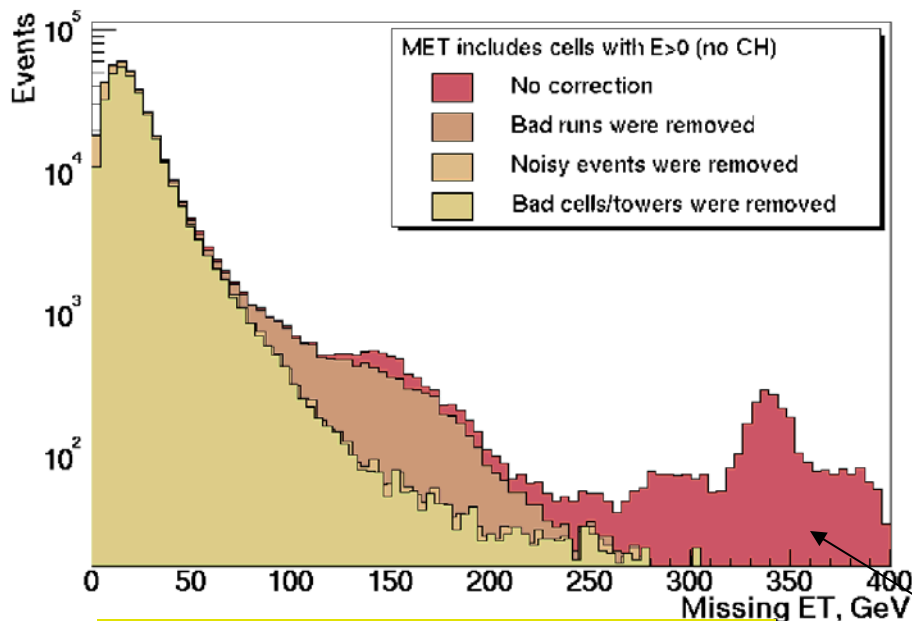


Different stages of MET

- L1 MET for triggering
- Corrected MET for analysis:
 - $\mu/e/\tau$ correction
 - vertex corrections
 - hot/dead channels
 - jet energy corrections
 - ...and many more.

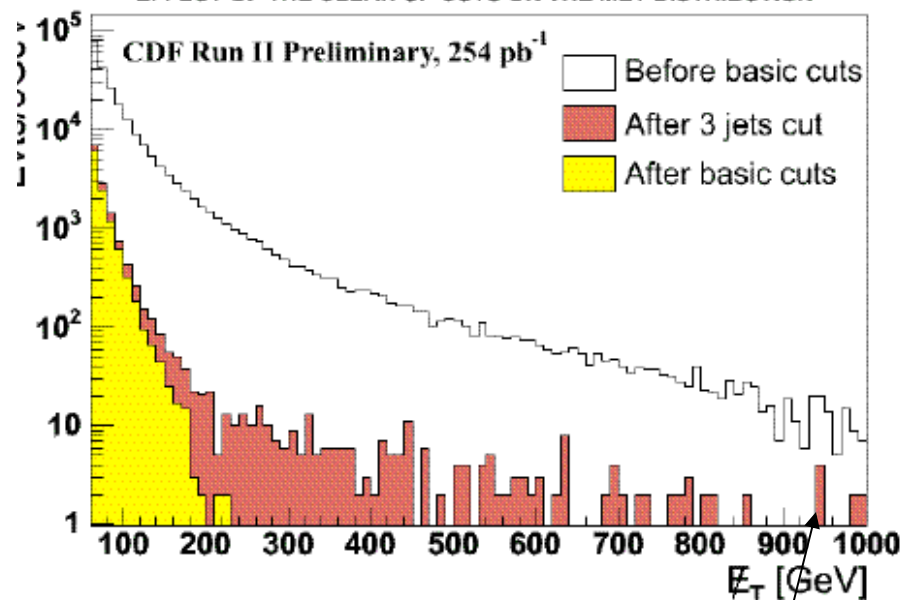
MET at Tevatron

Missing ET in MHT30 skim



MET, before corrections (D0)

EFFECT OF THE CLEAN UP CUTS ON THE MET DISTRIBUTION



MET, after corrections (CDF)

This is where new physics would sit



What physics with MET?

- Large MET (> 200 GeV)
 - Extra Dimension searches (monojet)
 - SUSY (gluino searches: jets+MET)
- Medium/Low MET ($\sim 50 - 100$ GeV)
 - Top quark
 - Ditalu
 - $H \rightarrow WW^*$
- Very Low MET (~ 20 GeV)
 - $W \rightarrow \ell \nu$

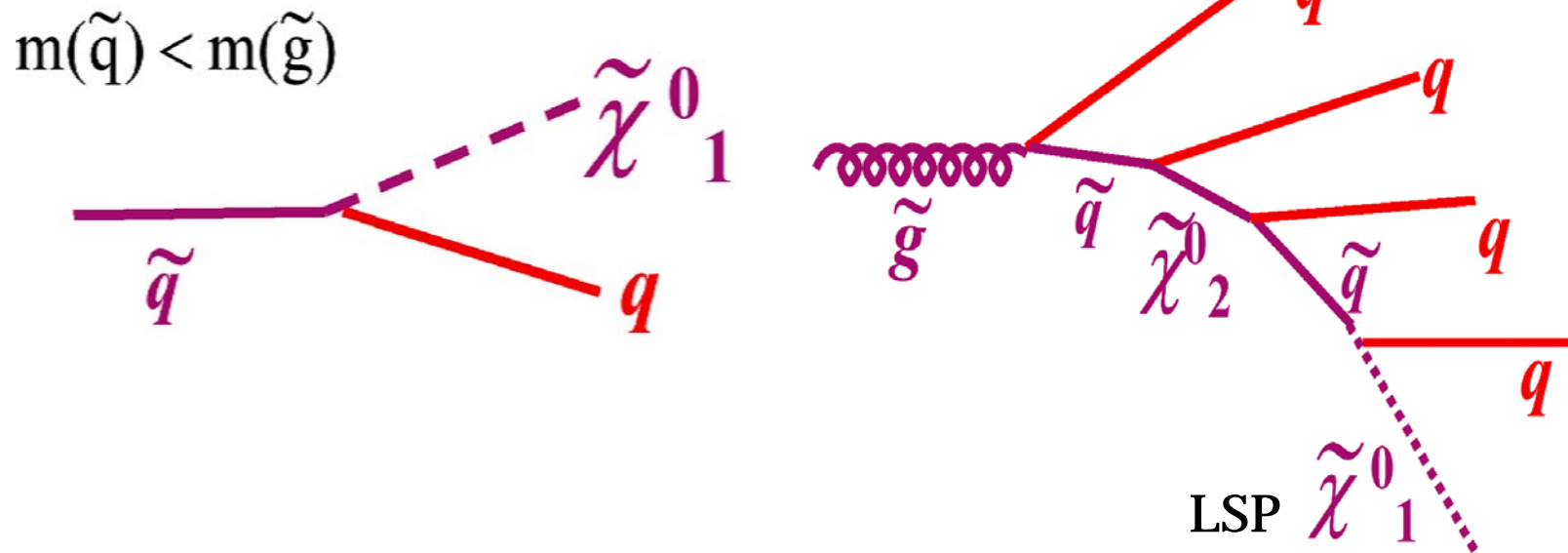


Physics with LARGE MET

Squark+gluinos with MET

If R-parity is conserved, LSP should give LARGE MET.

CMS Study: ≥ 3 jets with large MET (>200 GeV)
squark = 550 GeV, gluino = 600 GeV.



Squark + gluinos (CMS)

LM1 Test Point

$m(\text{gluino})=600 \text{ GeV}$
 $m(\text{squark})=550 \text{ GeV}$

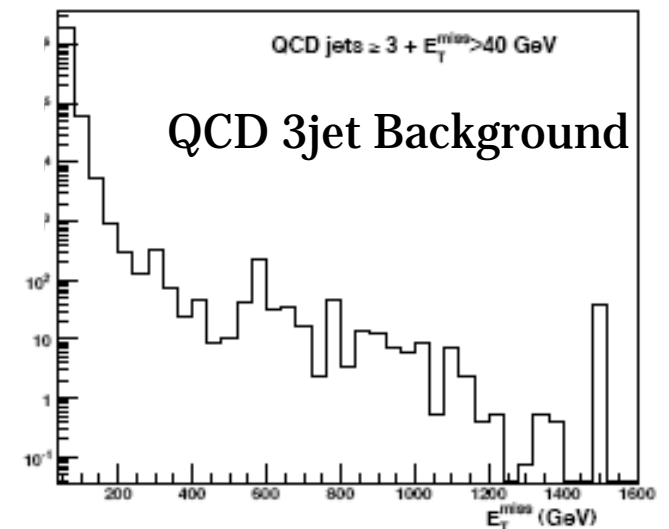
Table 4.2: The E_T^{miss} + multi-jet SUSY search analysis path

Requirement	Remark
Level 1	Level-1 trigger eff. parameter.
HLT, $E_T^{\text{miss}} > 200 \text{ GeV}$	trigger/signal signature
primary vertex ≥ 1	primary cleanup
$F_{em} \geq 0.175, F_{ch} \geq 0.1$	primary cleanup
$N_j \geq 3, \eta_d^{1j} < 1.7$	signal signature
$\delta\phi_{\min}(E_T^{\text{miss}} - \text{jet}) \geq 0.3 \text{ rad}, R1, R2 > 0.5 \text{ rad},$ $\delta\phi(E_T^{\text{miss}} - j(2)) > 20^\circ$	QCD rejection
$ISO^{\text{trk}} = 0$	ILV (I) W/Z/t \bar{t} rejection
$f_{em(j(1))}, f_{em(j(2))} < 0.9$	ILV (II), W/Z/t \bar{t} rejection
$E_{T,j(1)} > 180 \text{ GeV}, E_{T,j(2)} > 110 \text{ GeV}$	signal/background optimisation
$H_T > 500 \text{ GeV}$	signal/background optimisation
SUSY LM1 signal efficiency 13%	

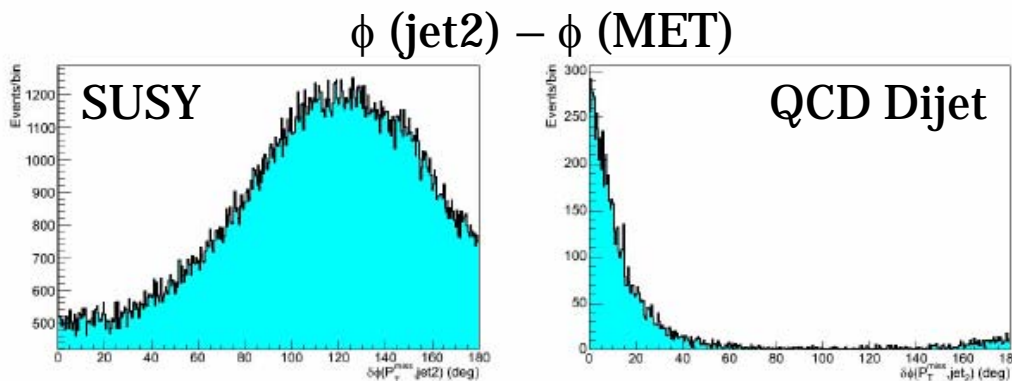
$\tilde{g}\tilde{q}$ is 53%, $\tilde{q}\tilde{q}$ 28% and $\tilde{g}\tilde{g}$ 12%.

$M_0 = 60 \text{ GeV}/c^2, M_{1/2} = 250 \text{ GeV}/c^2$.

$A_0 = 0, \mu > 0$ and $\tan \beta = 10$

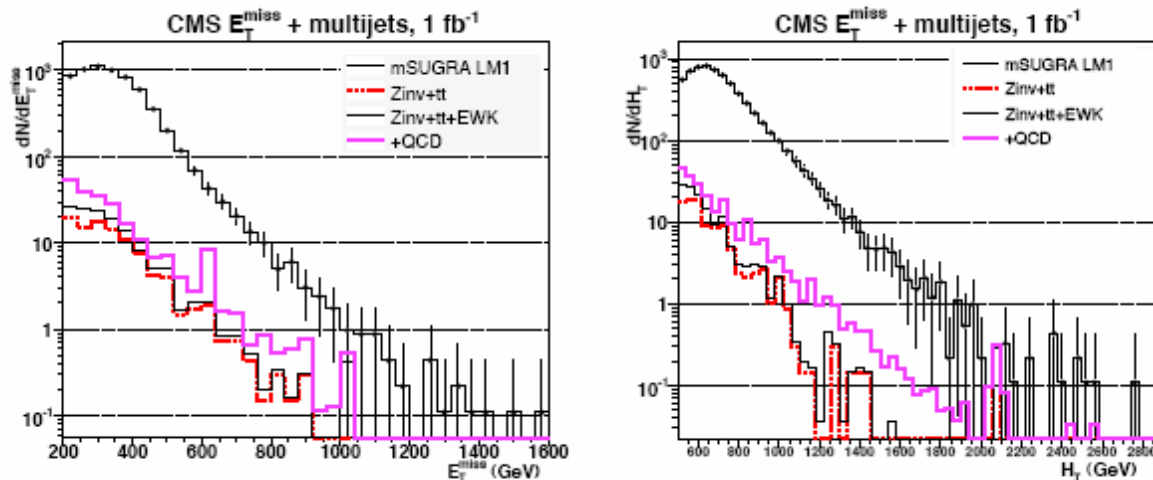


Squark gluino reach.

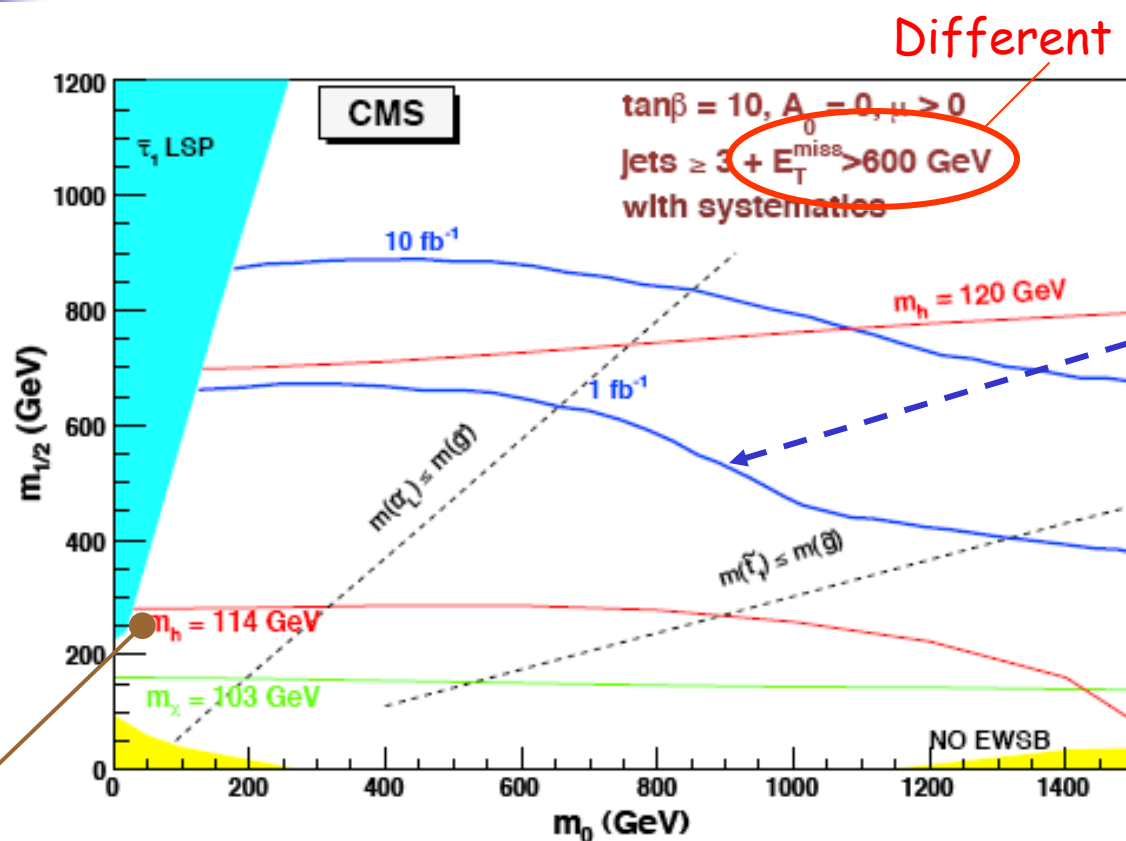


IF MET behaves, 5σ obs of low mass SUSY (Test point LM1) observable with 6pb^{-1} .

Figure 4.11: $\delta\phi_2 = |\phi_{j(2)} - \phi(E_T^{\text{miss}})|$ for (left) SUSY signal and (right) QCD dijet events



SUSY reach



Different cut, higher MET

Effective coverage of most low-mass SUSY space.

IF R-parity is conserved...

LM1 Test Point

Extra Dimensions (ADD)

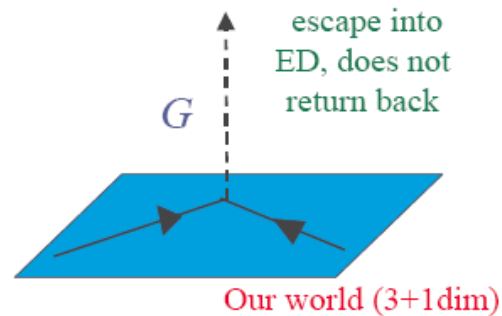
Large Extra Dimensions (ADD) Model

(“ADD” => N. Arkani-Hamed, S. Dimopoulos, and G.Dvali)

- $M_{Pl}^2 \sim R_c^n M_D^{2+n}$
 - M_{Pl} : Planck scale
 - R_c : radius of ED
 - M_D : new effective fundamental scale
 - n : # extra dimensions
- Large extra dimension : $R \sim 1\text{mm}$ for $n=2$, $M_D \sim 1\text{TeV}$
- Kaluza-Klein states of Graviton is dense and evenly spaced
 - Mass spectrum appear continuous
 - Interfere with SM scattering amplitude

Direct G emission :

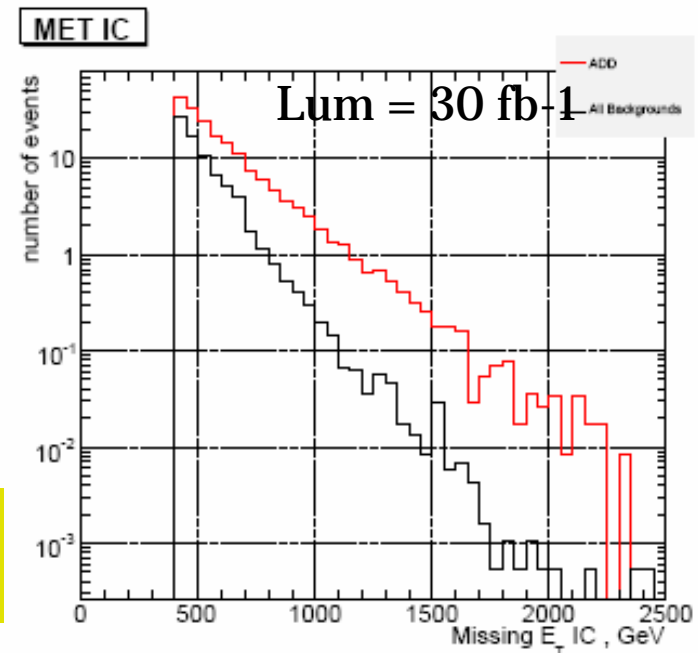
$$\begin{array}{l}
 q \bar{q} \rightarrow \gamma G \\
 q \bar{q} \rightarrow Gg \\
 qg \rightarrow Gq \\
 gg \rightarrow Gg
 \end{array}
 \left. \begin{array}{l}
 \text{Photon} \\
 +\text{MET} \\
 \\
 \text{jet+} \\
 \text{MET}
 \end{array} \right\}$$



LED: Photon + MET

- Photon $p_t > 400$ GeV
- MET > 400 GeV
- $\Delta\phi(\text{photon}, \text{MET}) > 2.5$
- No tracks > 40 GeV

$M_d = 2.5$ TeV
 $n=2$





LED Reach Photon+MET

M_D : Fundamental Plank mass; $n = \#$ ED.

M_D/n	$n = 2$	$n = 3$	$n = 4$	$n = 5$	$n = 6$
$M_D = 1.0$ TeV	0.21 fb ⁻¹	0.16 fb ⁻¹	0.14 fb ⁻¹	0.15 fb ⁻¹	0.15 fb ⁻¹
$M_D = 1.5$ TeV	0.83 fb ⁻¹	0.59 fb ⁻¹	0.56 fb ⁻¹	0.61 fb ⁻¹	0.59 fb ⁻¹
$M_D = 2.0$ TeV	2.8 fb ⁻¹	2.1 fb ⁻¹	1.9 fb ⁻¹	2.1 fb ⁻¹	2.3 fb ⁻¹
$M_D = 2.5$ TeV	9.9 fb ⁻¹	8.2 fb ⁻¹	8.7 fb ⁻¹	9.4 fb ⁻¹	10.9 fb ⁻¹
$M_D = 3.0$ TeV	47.8 fb ⁻¹	46.4 fb ⁻¹	64.4 fb ⁻¹	100.8 fb ⁻¹	261.2 fb ⁻¹
$M_D = 3.5$ TeV	5 σ discovery not possible anymore				

TeV scale reached
well below 1 fb⁻¹.



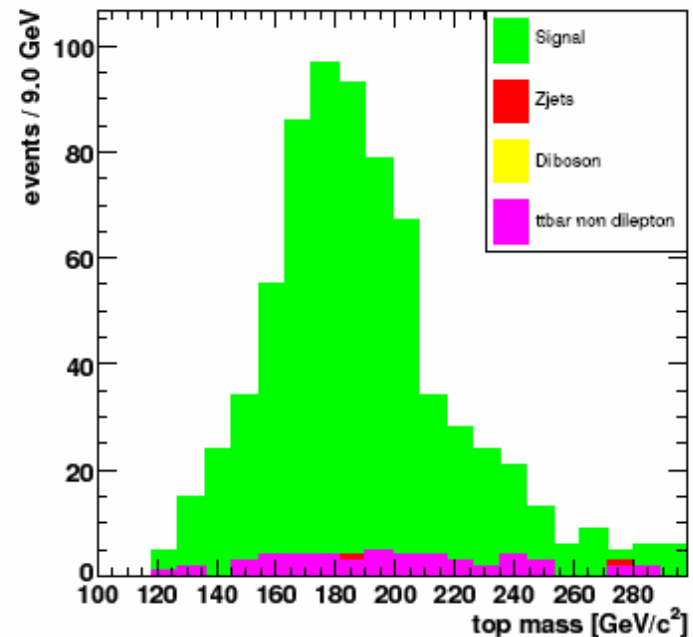
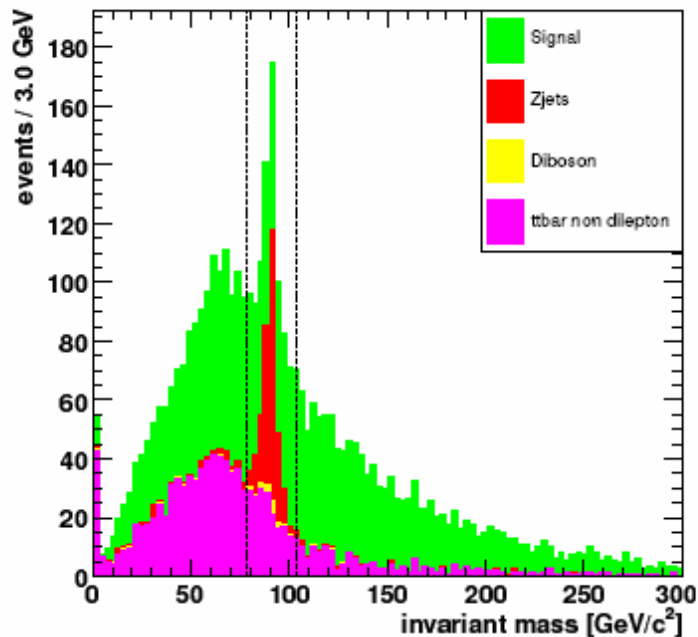
Medium /Low MET Analyses

Di-Leptonic $t\bar{t}$ (CMS)

LO(pb)

	Signal	τ	WW	WZ	ZZ	Z + jets	other $t\bar{t}$
Before selection	24.3	30.4	7.74	0.89	0.11	3912	438
Level-1 + HLT	19.4	15.1	4.4	0.37	0.07	657	92
2 jets $E_T > 20$ GeV	11.5	9.8	0.6	0.012	0.006	23.9	73.1
$E_T^{\text{miss}} > 40$ GeV	9.6	8.1	0.5	0.01	0.003	5.8	53.6
Two opp. charged leptons	3.2	0.42	0.04	0.001	0.001	1.17	0.12
b-tag of two highest E_T jets	1.12	0.15	0.002	$\sim 10^{-4}$	$\sim 10^{-5}$	< 0.01	0.05

Only slight improvement in background rejection



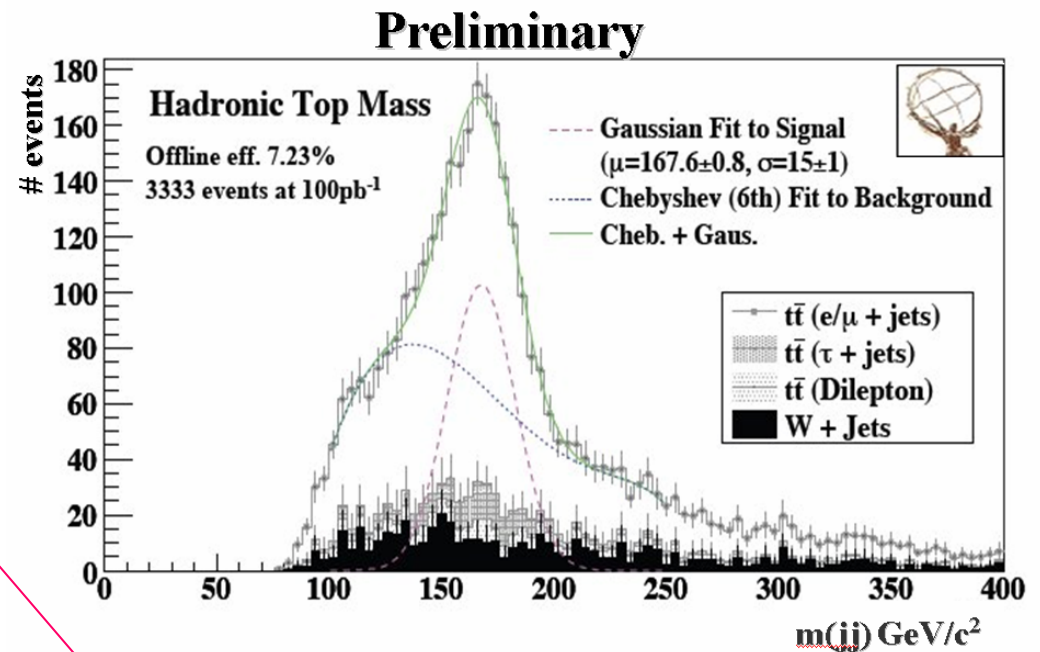
Semi Leptonic $t\bar{t}$ bar (ATLAS)

Selection A

- 1 high- p_T lepton > 20 GeV/c
- at least 3 high- p_T jets > 40 GeV/c
- 1 high- p_T jets > 20 GeV/c
- ET miss > 20 GeV
- $|\eta(\text{lepton})| < 2.4$, $|\eta(\text{jet})| < 2.5$
- top is reconstructed as the 3-jet combination with the highest PT sum

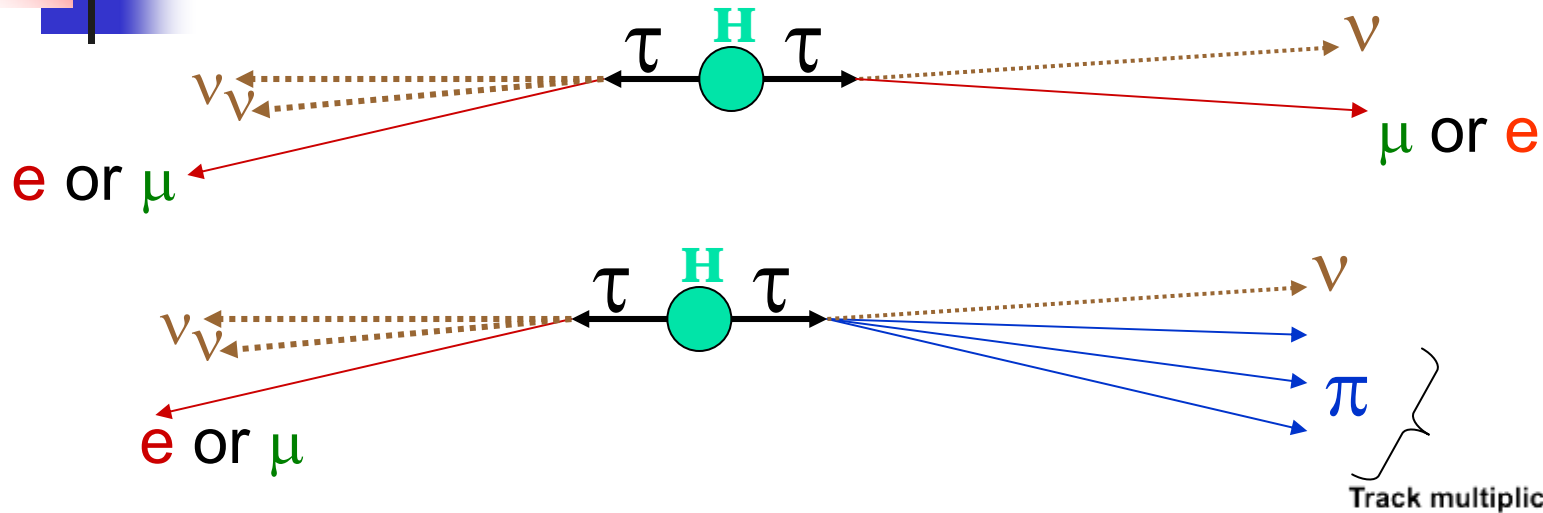
Selection B

- Same as selection A
- additional cut $|m_{jj} - M_W| < 10$ GeV

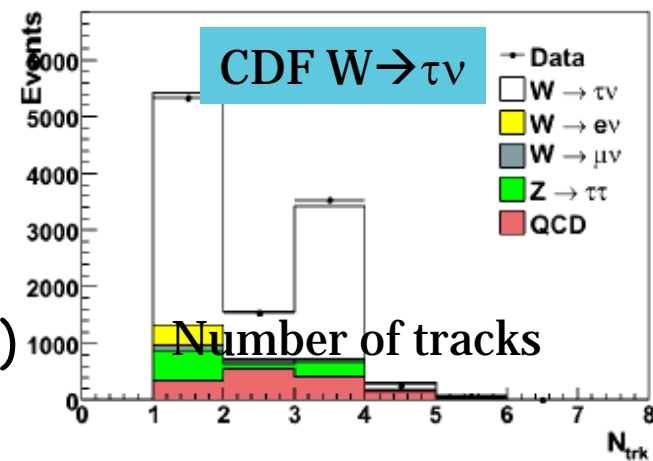


At (below?) resolving power of MET

Ditau analyses

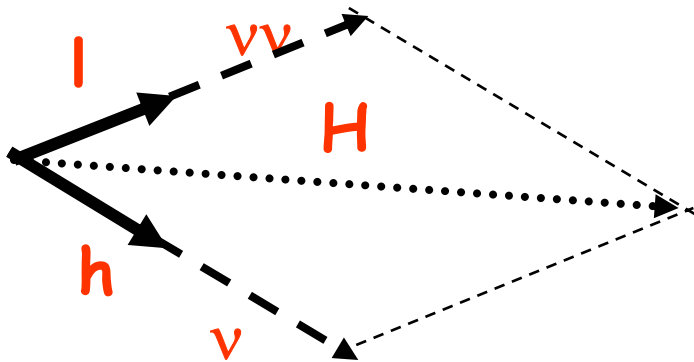


- Identifying hadronic tau is possible
 - Nested signal/isolation cones
- Need to separate from Z
 - M_{vis} (used in CDF, broad dist)
 - Invariant mass (no back-to-back taus)



Ditau invariant mass

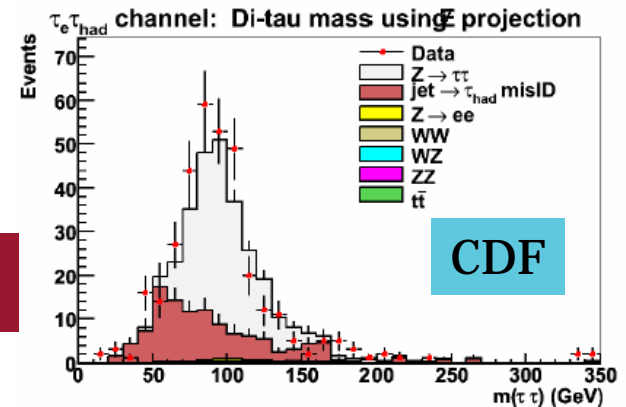
Assume tau decay products are collinear to tau directions - aka "projection method".



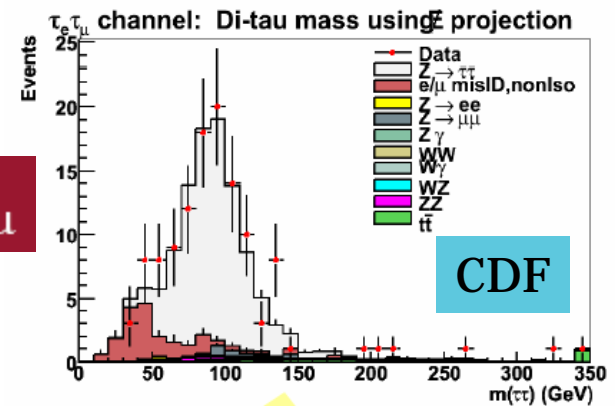
Requires good resolutions at low MET.

Does it work?
CDF 1.8 fb⁻¹ results

$\tau_e \tau_{had}$



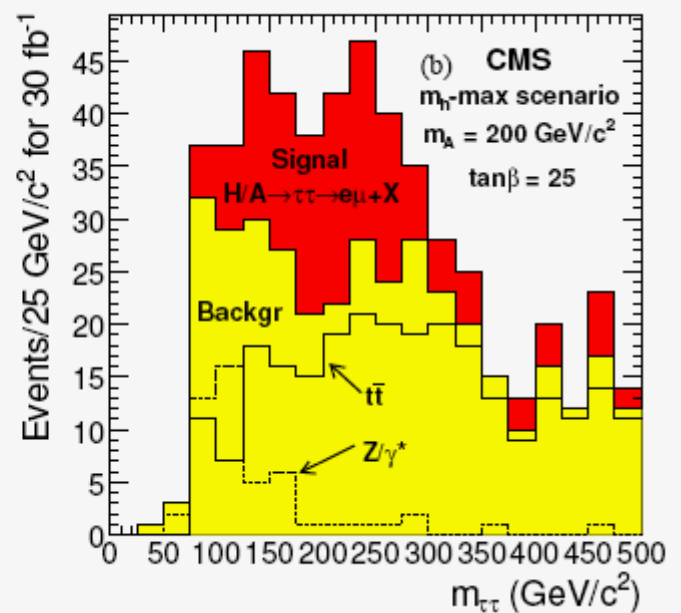
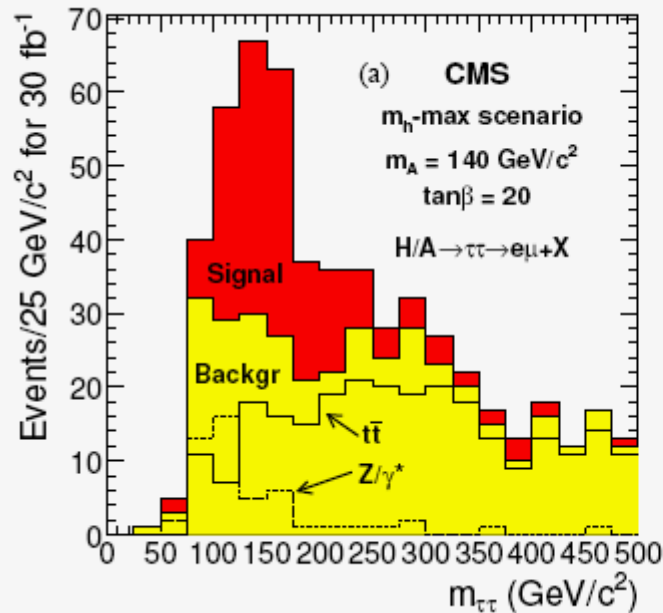
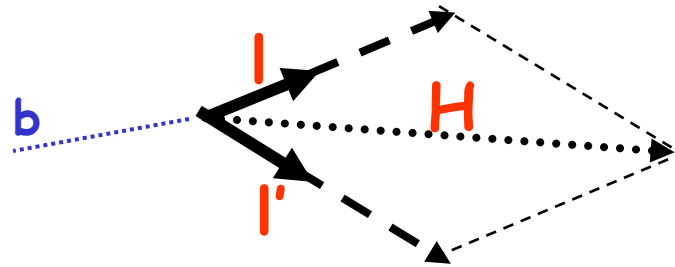
$\tau_e \tau_\mu$



$\tau\tau$ invariant mass

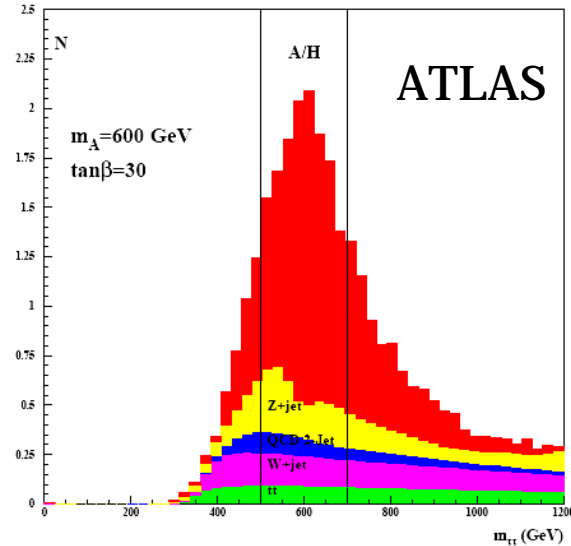
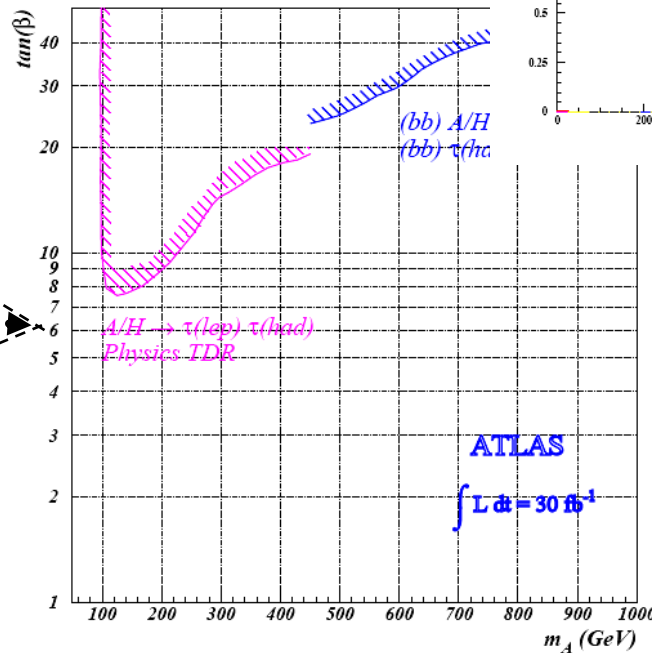
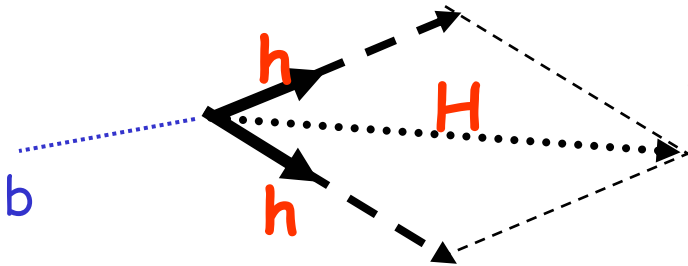
Higgs \rightarrow ditau (CMS)

- 2 isolated leptons
- 1 b-tag (but associated b is soft)
- Only 1 extra central jet
- **NO MET cut (but used in mass reco)**
- Positive solution to ν energy



Higgs to ditau (ATLAS)

- 1. Two (had) τ 's $p_T; > 100$ GeV
- 2. No lepton with $p_T > 10$ GeV
- 3. ≤ 4 jets in with $p_T > 20$ GeV
- 4. At least one b-jet tagged
- 5. **MET > 65 GeV**
- 6. $D_{\phi} b \tau\text{-}\tau$: 145 – 175 deg
- 7. $m_T < 50$ GeV
- 8. $\tau\tau$ mass recon possible



H → WW*

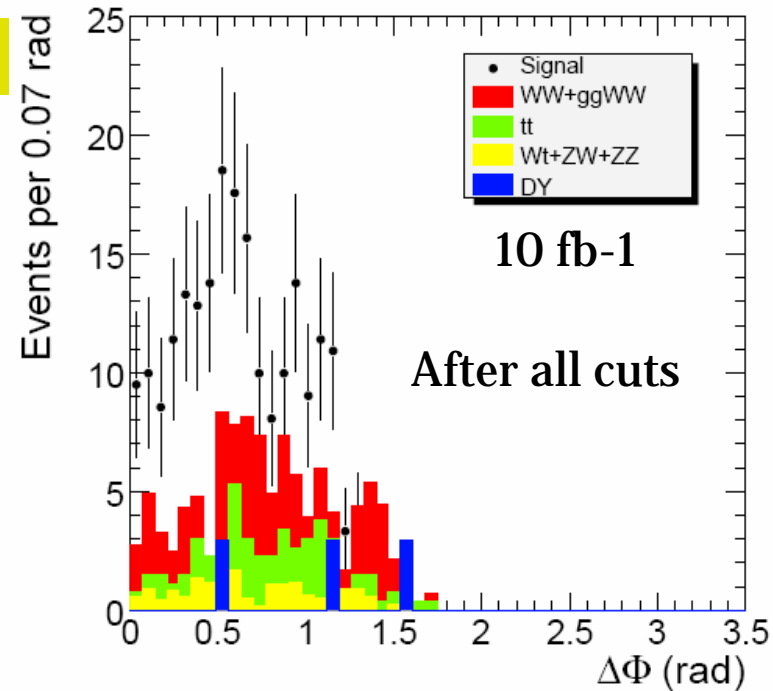
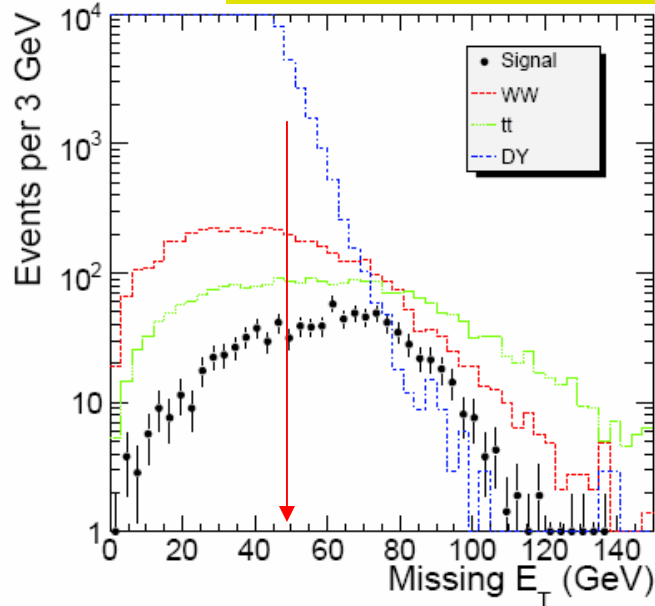
$$q \bar{q} \rightarrow W^+ W^- \rightarrow 2\mu 2\nu$$

$$g g \rightarrow t \bar{t} \rightarrow 2\mu 2\nu$$

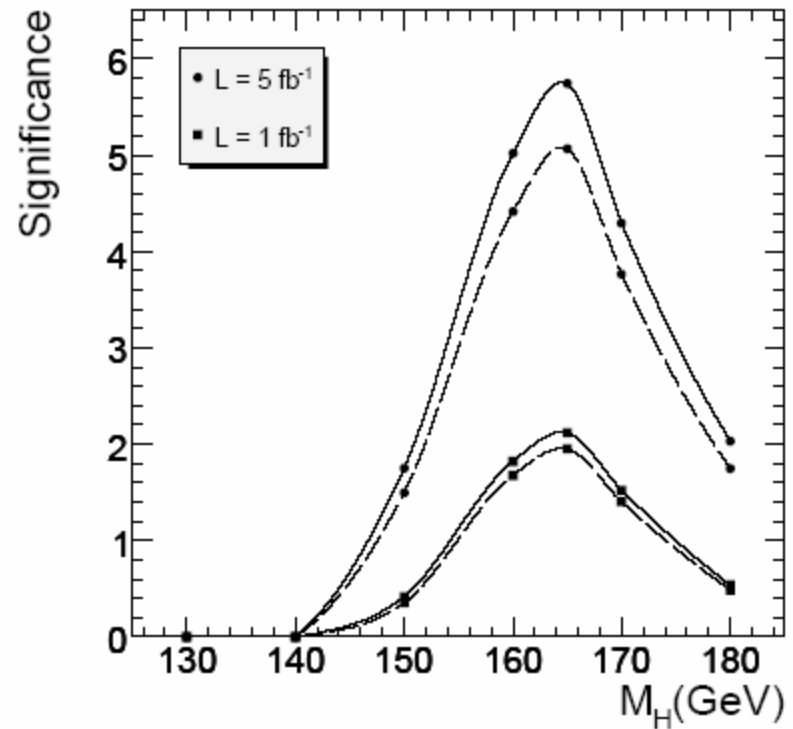
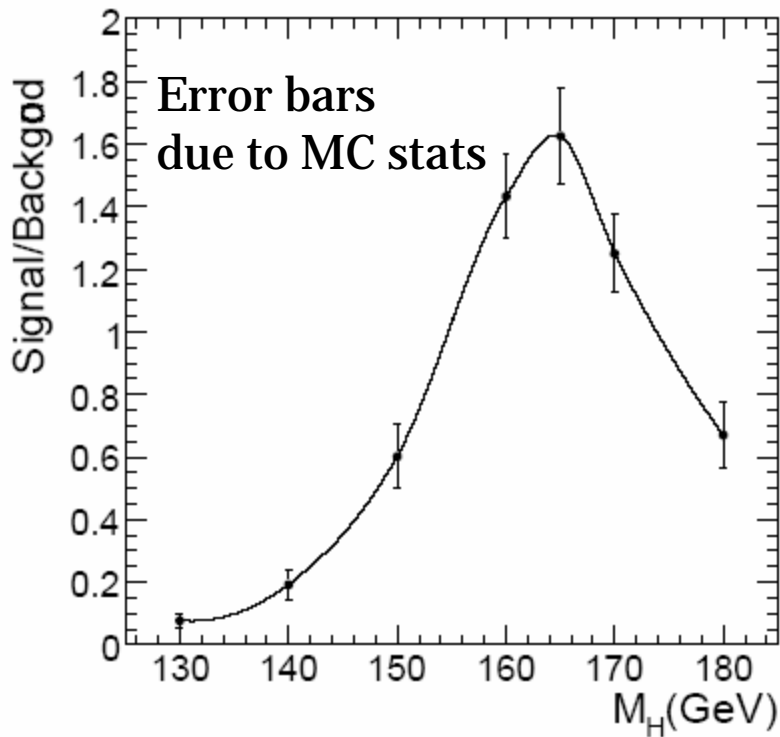
$$q \bar{q} \rightarrow \gamma^*, Z \rightarrow 2\mu$$

1	L1+HLT dimuon	6	MET > 50 GeV
2	2 μ opposite charge	7	$35 \text{ GeV}/c < P_T(\mu_{max}) < 55 \text{ GeV}/c$
3	Isolation	8	$25 \text{ GeV}/c < P_T(\mu_{min})$
4	$\eta < 2.0$ $IP < 3\sigma$	9	$m_{\mu_1\mu_2} < 50 \text{ GeV}/c^2$
5	Jet Veto	10	$\Delta\phi_{\mu_1\mu_2} < 0.8$

Optimized for $m_h = 165 \text{ GeV}$



H \rightarrow WW* reach



MET Concerns

■ Resolution

- **Noise:** electronic underlying event
- **Stochastic:** sampling effects, e/π .
- **Constant:** non-linearities, cracks, hot/dead channels.
- **Offset:** ΣE_T shifts in empty detector (anticorrelated with Noise term).

$$\sigma(E_T) = A \oplus B\sqrt{\Sigma E_T - D} \oplus C (\Sigma E_T - D)$$

noise

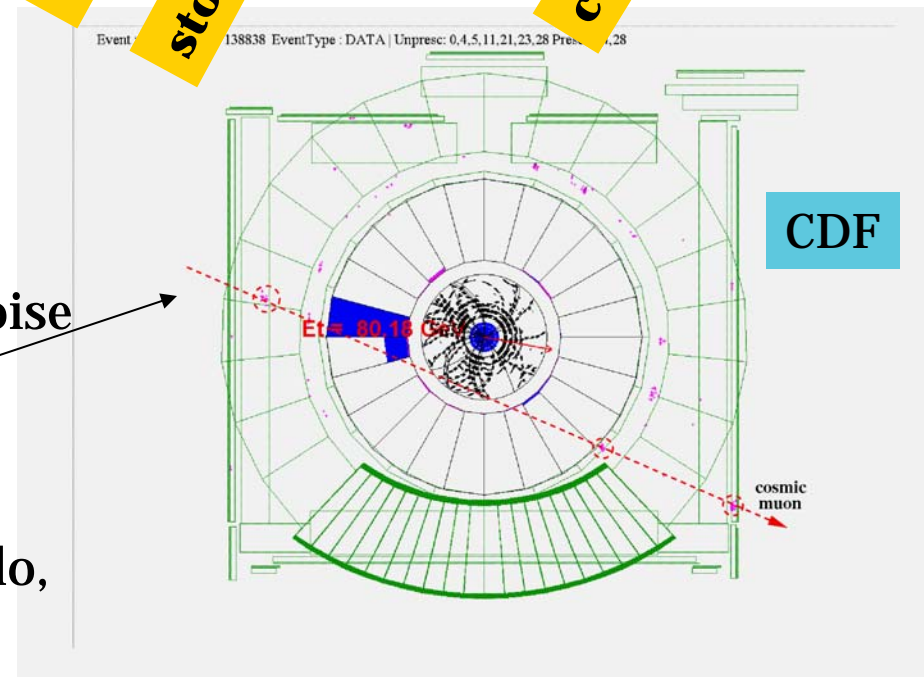
stochastic

constant

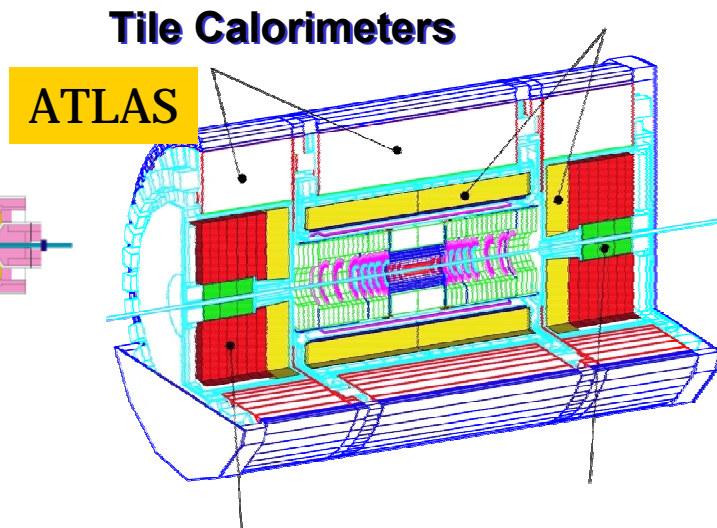
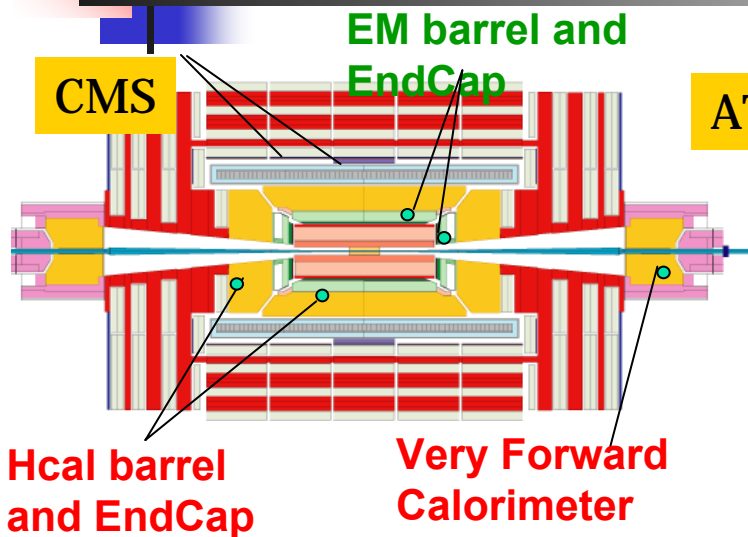
offset

■ High MET Tails

- Beam effects, muon halo, cosmics...



Calorimeter η coverage



EM calorimeter $|\eta| < 3$
Central Hadronic $|\eta| < 1.4$
Endcap Hadronic $1.3 < |\eta| < 3$
Forward calorimeter $2.9 < \eta < 5$

EM accordion $|\eta| < 3.2$
Central Hadronic $|\eta| < 1.7$
End Cap Hadronic $1.5 < \eta < 3.2$
Forward cal $3.1 < \eta < 4.9$

Central $|\eta| < 1.0$
Plug $1.3 < |\eta| < 3.6$

Better eta coverage → Better performance on MET const term.

better

more

Segmentation, interaction lengths

CMS

EM calorimeter $|\eta| < 3$:
PbW04 crystals
 $\Delta\eta \times \Delta\phi = \mathbf{0.0174 \times 0.0174}$

Central Hadronic $|\eta| < 1.7$
Brass/scintillator
 $\Delta\eta \times \Delta\phi = \mathbf{0.087 \times 0.087}$

Endcap Hadronic $1.3 < |\eta| < 3$
Brass/scintillator +WLS
 $\Delta\eta \times \Delta\phi = \sim \mathbf{0.15 \times 0.17}$

Forward calorimeter
 $3 < \eta < 5$
Fe/quartz fibers
 $\Delta\eta \times \Delta\phi = \sim \mathbf{0.175 \times 0.17}$

ATLAS

EM accordion
 $|\eta| < 3.2$:Pb/LAr
 $\Delta\eta \times \Delta\phi \sim \mathbf{0.025 \times 0.025}$

Central Hadronic
 $|\eta| < 1.7$:Fe / scint
 $\Delta\eta \times \Delta\phi \sim \mathbf{0.1 \times 0.1}$

End Cap Hadronic
 $1.5 < \eta < 3.2$ Cu/LAr
 $\Delta\eta \times \Delta\phi < \mathbf{0.2 \times 0.2}$

Forward calorimeter
 $3.1 < \eta < 4.9$:
EM Cu/LAr – HAD W/Lar
 $\Delta\eta \times \Delta\phi = \mathbf{0.2 \times 0.2}$

CDF

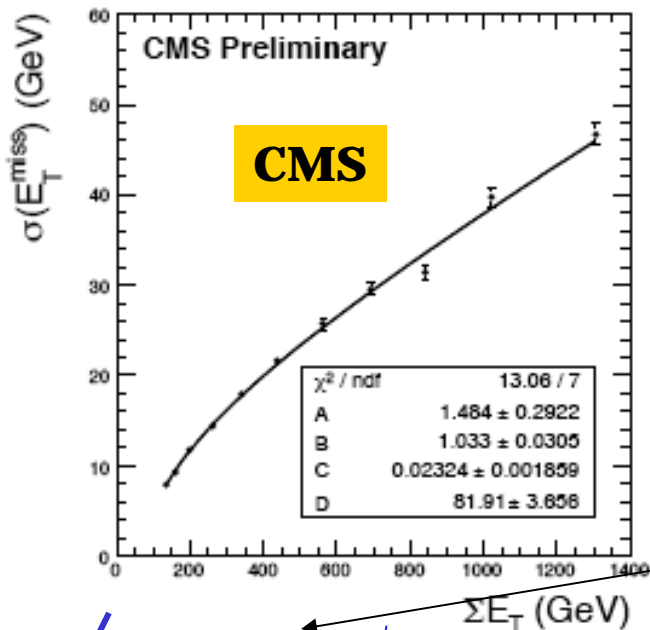
Central $|\eta| < 1.0$
 $\Delta\eta \times \Delta\phi \sim \mathbf{0.11 \times 0.26}$

Plug $1.3 < |\eta| < 3.6$
 $\Delta\eta \times \Delta\phi$
from $\sim 0.11 \times 0.13$
to $\sim 0.36 \times 0.26$

CDF 5,5 - 7 λ

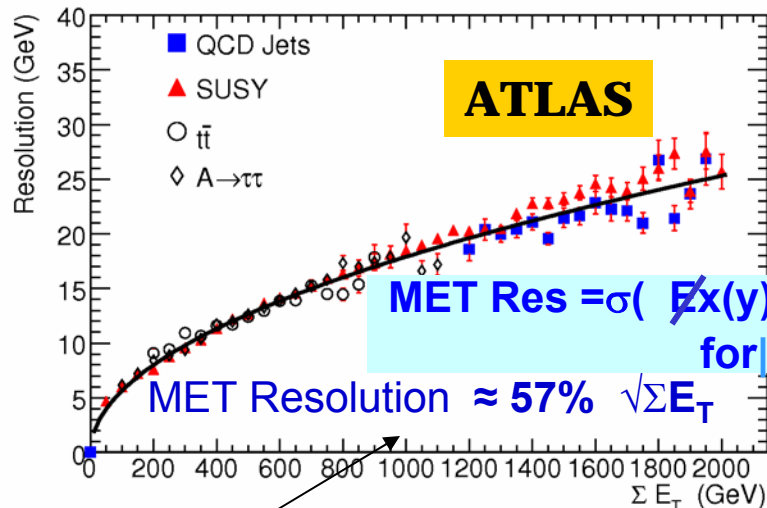
CMS cal has 7λ (w/out HO). ATLAS cal has $\geq 10 \lambda$

MET Performance (stochastic term)



$$\sigma(\cancel{E}_T) \approx 103\% \sqrt{\Sigma E_T} + \dots$$

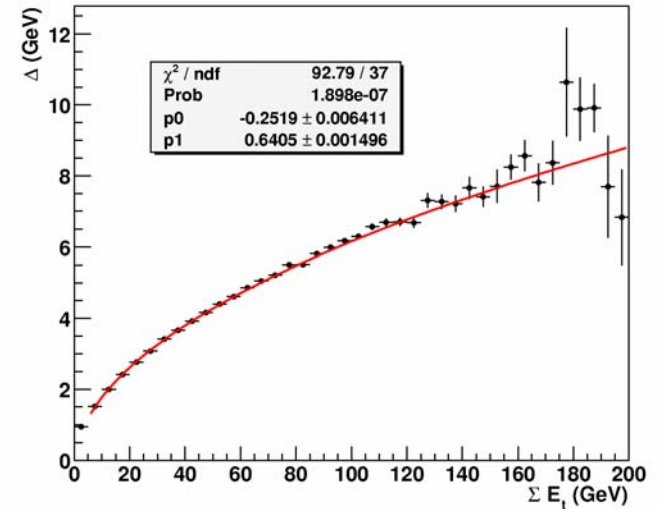
$$\begin{aligned} \sigma^2(\cancel{E}_T) &= (1.48 \text{ GeV})^2 \\ &+ (103\% \text{ GeV}^{1/2})^2 (\Sigma E_T - 82 \text{ GeV}) \\ &+ (2.32\% \times (\Sigma E_T - 82 \text{ GeV}))^2. \end{aligned}$$



Not an apples-to-apples comparison...

ATLAS cal has more longitudinal segmentation: (e/pi)

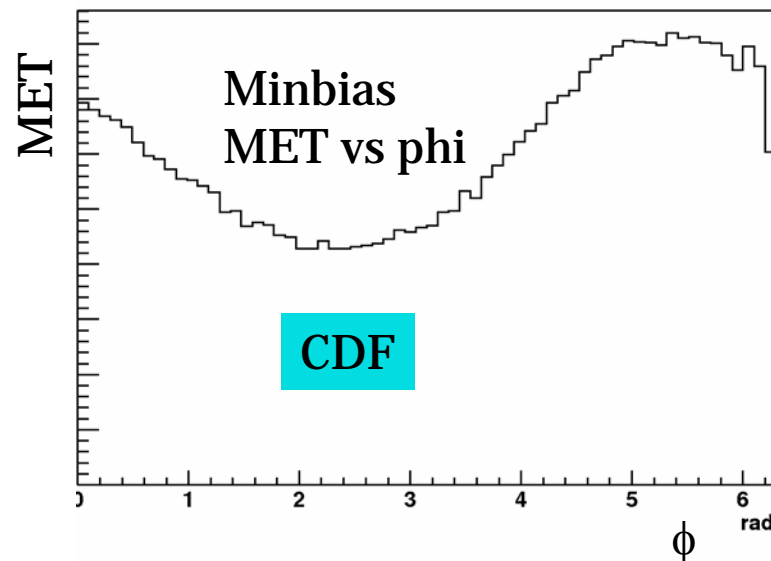
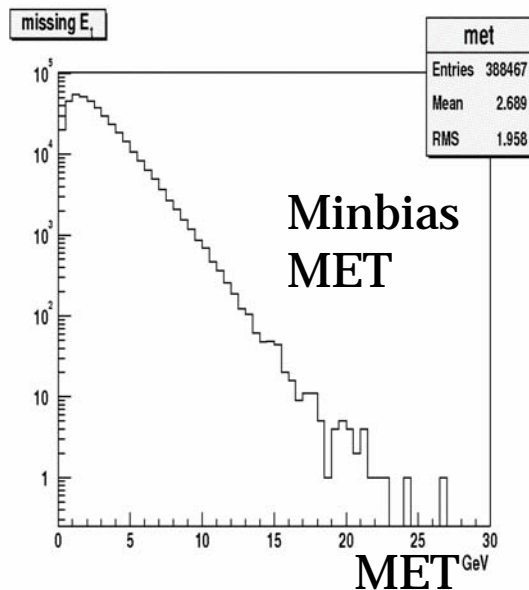
Minbias data, underestimate stochastic term.





Some MET Peculiarities from CDF

MET Peculiarities



MET has a phi dependence ~ few GeV.
→ collision not centered at 0,0,0.

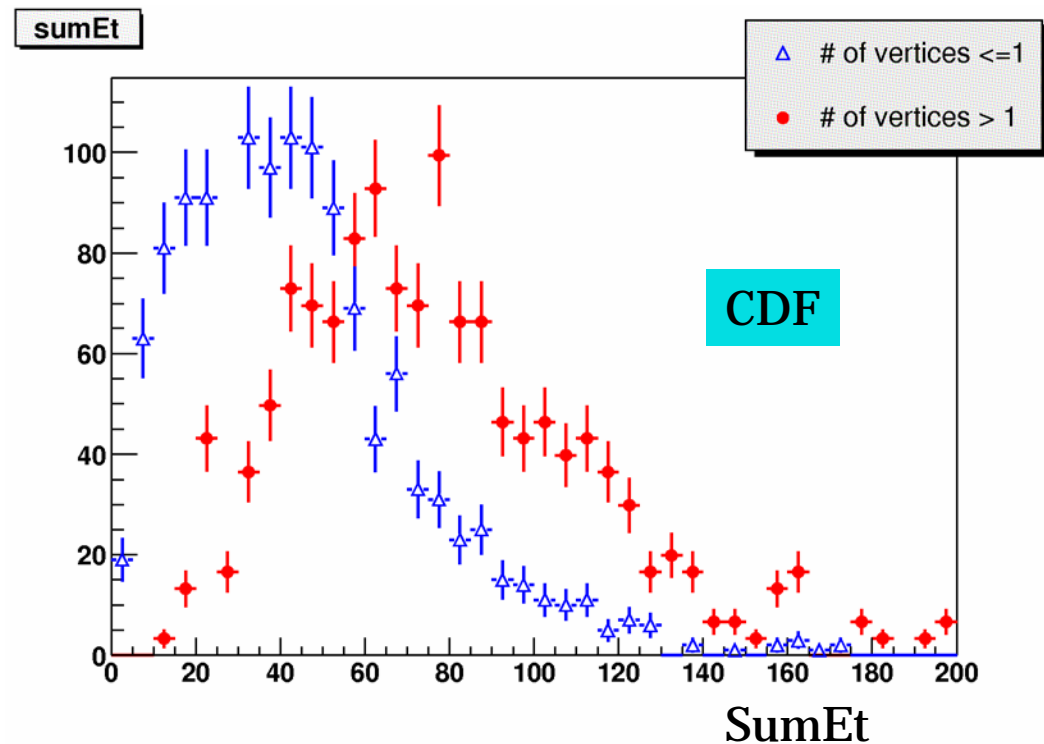
MET Peculiarities

SumEt from $Z \rightarrow \mu\mu$ events

Events with 2nd vertex have significantly higher SumEt.

Jets from 2nd vertex could affect MET calculation.

This will depend on lum, but non-trivial numbers at low luminosity.



Hopefully not as big a problem at LHC (smaller beam ellipse than Tevatron)

MET Peculiarities

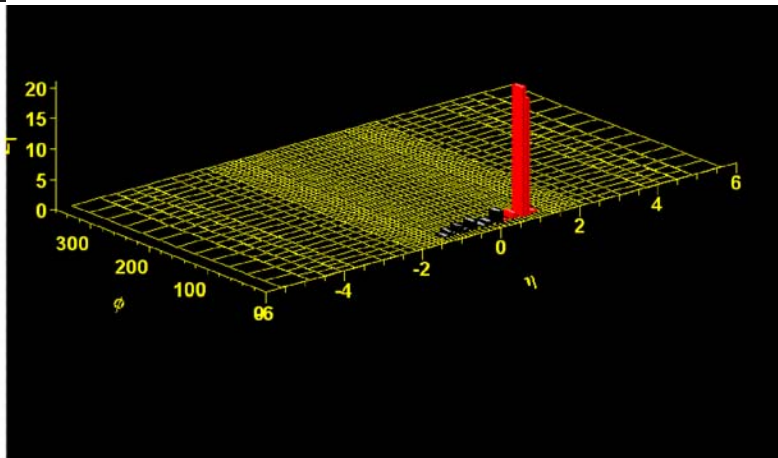
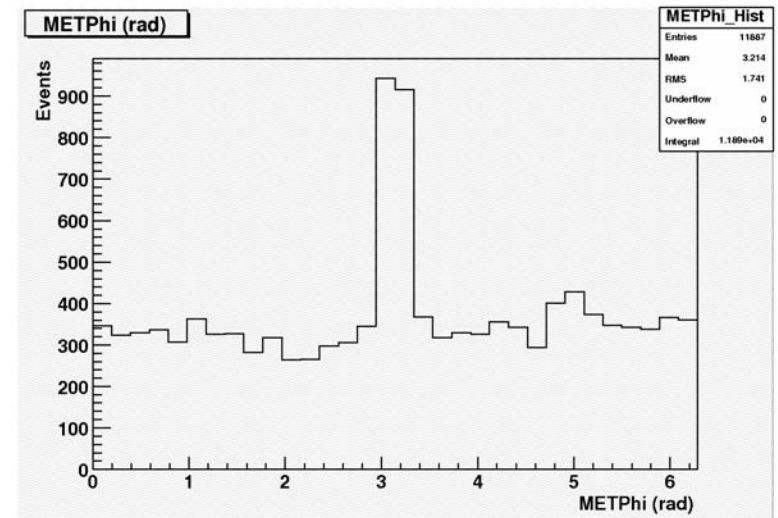


Figure 1: An $\eta - \phi$ plot of the energy in the calorimeter towers of a bunch crossing event that has a halo muon traversing through the central calorimeter in the direction parallel to the beam axis.



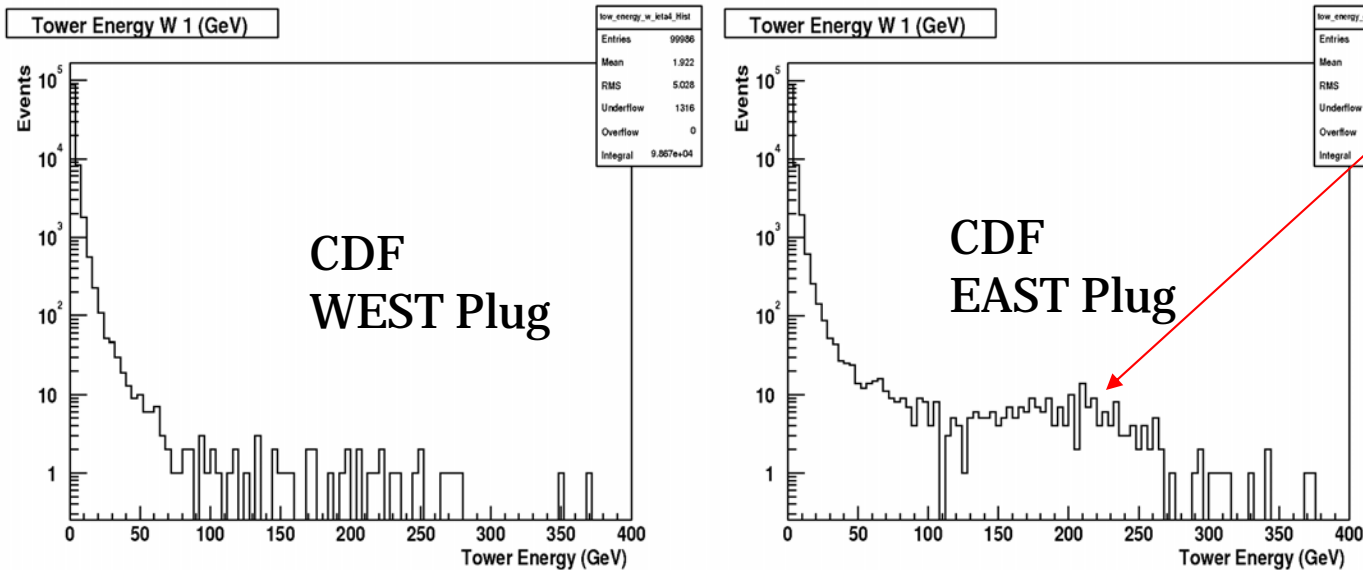
Beam halo muons can deposit large amounts of IN-TIME energy.

EM/HAD ratio is fairly lopsided.



MET Peculiarities

Energy deposited in the **Ring of Fire** (highest eta towers)



Tevatron protons travel W \rightarrow E. So EAST Plug energy is in time.

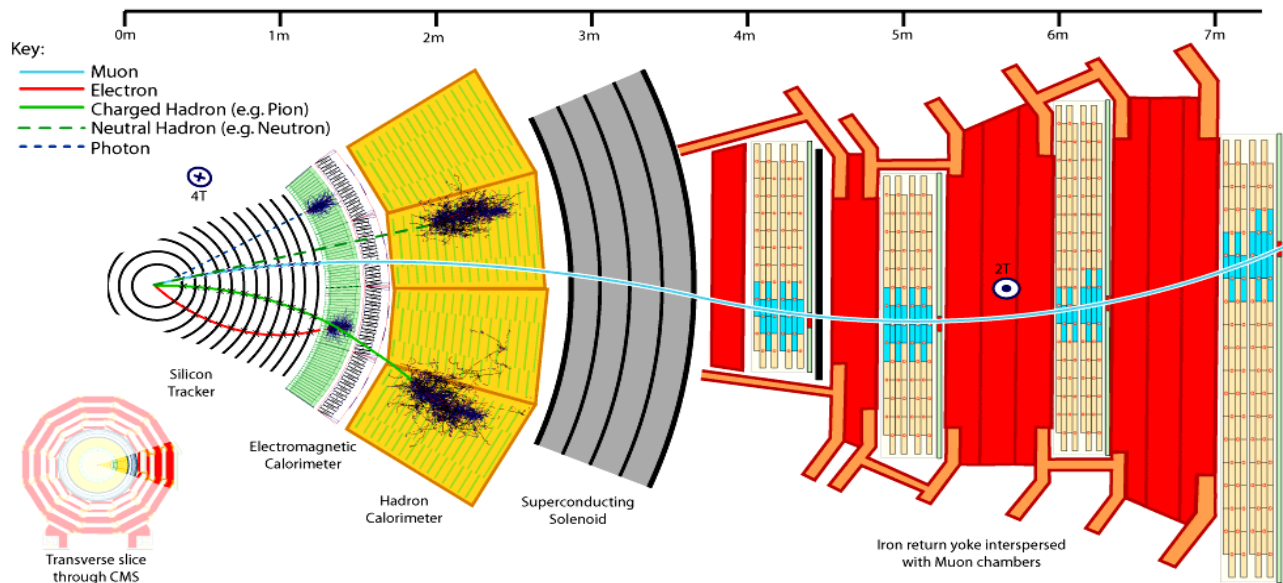
W Plug should get pbars in time, but pbar flux is small.

Figure 5: Plots on the energy of the towers in the highest η -ring for events taken with Pass2 MET25 trigger (with Level-2 and Level-3 pass through). (Left) Towers from the west Plug calorimeter. (Right) Towers from the east Plug calorimeter.



Particle Flow: Improving MET

Particle Flow



Current MET: all calorimeter (+muon correction)

Particle Flow:

Biggest problem in MET: hadron energy.

Identify e , γ , π , μ , charged/neutral hadrons, pileup, etc, and "correct".

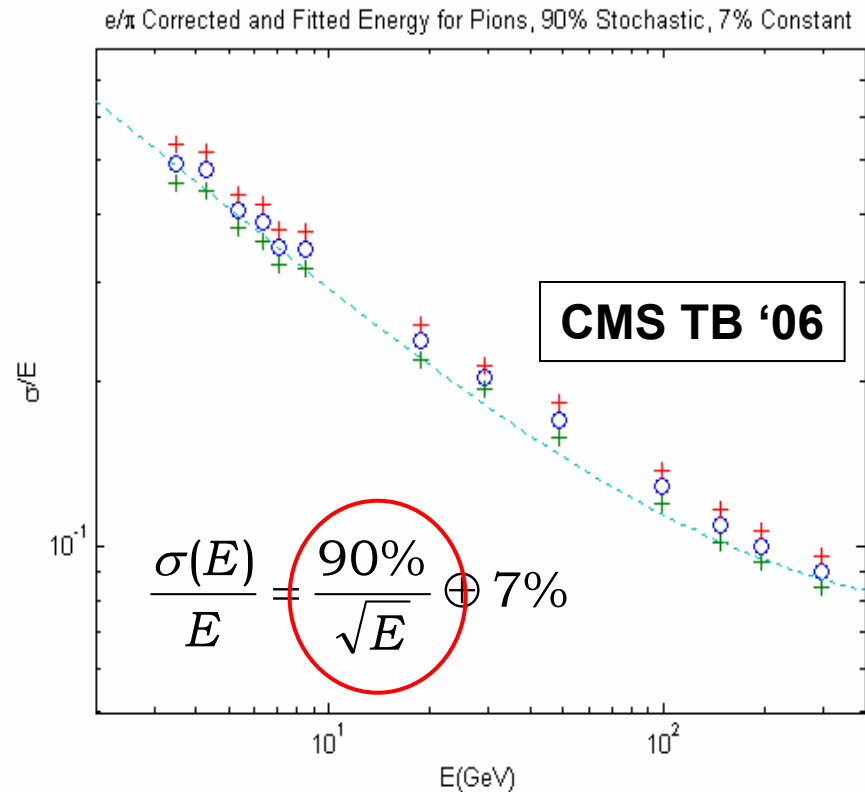
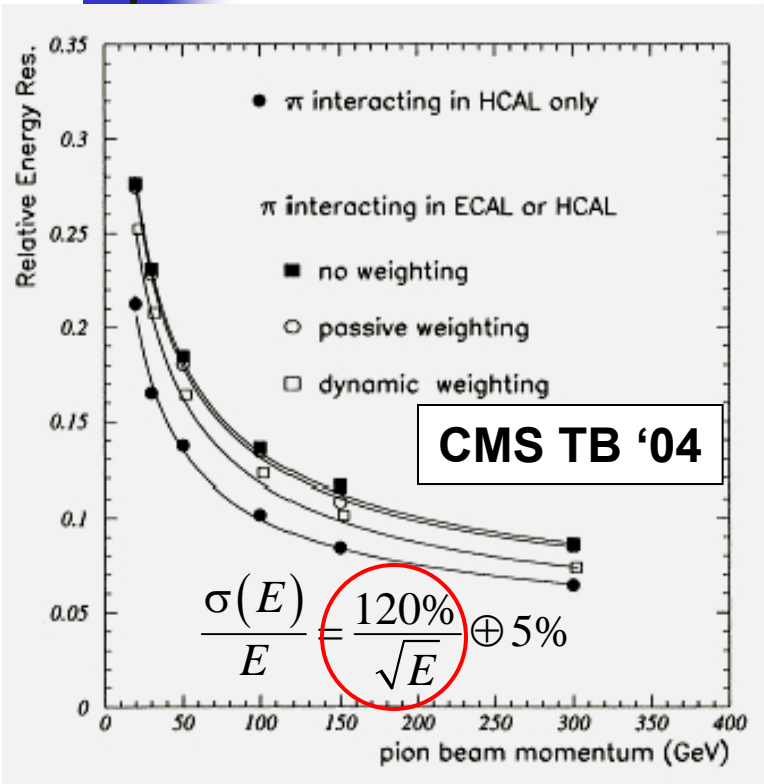
Harder in jetty environment, but what isn't?



Benefits of Particle flow

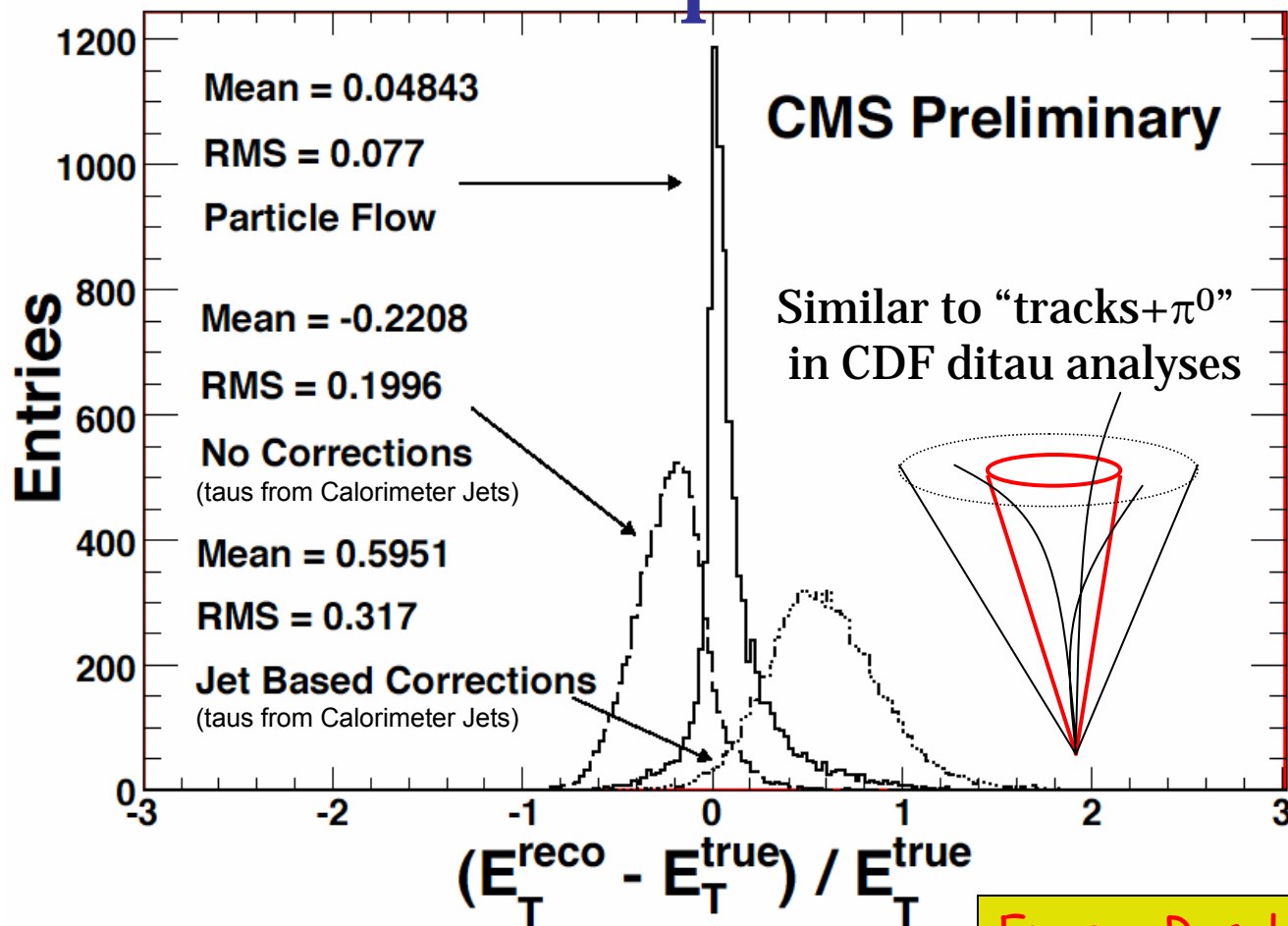
- **Motivation: The energy of a typical jet consists roughly of**
 - **Charged particles : ~60%**
 - Mostly charged pions, kaons and protons, but also some electrons and muons
 - **Photons : ~25%**
 - Mostly from π^0 's, but also some genuine photons (brems,...)
 - **Long-lived neutral hadrons : ~10%**
 - K_L^0 , neutrons
 - **Short-lived neutral hadrons, “ V^0 's” : ~5%**
 - $K_S^0 \rightarrow \pi^+\pi^-$, $\Lambda \rightarrow \pi^-p$, ..., but also γ conversions, and (more problematic) nuclear interactions in the detector material.
- **Energy resolution determined (ideally) mostly by**
 - the 10% neutral hadrons
 - inefficiencies in charged hadron reconstruction
- **Attempt to use Full Detector/Event Information in MET reconstruction**
 - Determine MET from calibrated, reconstructed particles

Improving e/ π helps!



Good beam conditions in 2006
combined with very clean Particle ID

PF Example: hadronic τ energy



Energy Resolution Improves!

- Calorimeter Jets strongly affected: low energy charged particles not
- PF Jets not affected much in the peak.
- Better energy resolution for objects using tracking info \rightarrow better SumEt, MET resolution.
- **Acid test:** very jetty, noisy environments.



Summary

- MET is as difficult to reconstruct as it is important.
 - Current MET resolutions are only starting points.
 - Expect ATLAS vs CMS differences to get smaller
 - CMS learns to use tracking (PF).
 - Of course, ATLAS will also keep improving...
 - **Bottom line: ATLAS has better cal; CMS: better tracking.**
- **Biggest problems in MET reconstruction will not be known until beams collide.**
 - Look for beam effects, dead/hot channels, miscalib...
- Once MET is understood, lots of analyses benefit: low mass SUSY, LED, ditaus...



Backup stuff

ATLAS vs. CMS MET

- ATLAS constant term \sim zero.
- CMS stochastic higher than ATLAS stochastic (but ATLAS quotes MET reco-truth...):

ATLAS has

- 6 radial cal segments
- e/π ratio closer to 1
- (slightly) more λ
- Object based calib (em, had, other...)
- CMS will need to use tracking info to compete (Particle Flow)

- Other effects (dead/hot channels)

